\ll Analyse complexe et la théorie du potentiel \gg Un colloque en l'honneur de Paul M. Gauthier et Kohur Gowrisankaran

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Extensions of the disc algebra

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We determine the set $\tilde{A}(D)$ of uniform limits of polynomials on the closed unit disc \overline{D} with respect to the chordal metric χ on $\mathbb{C} \cup \{\infty\}$. We study properties of the elements of $\tilde{A}(D)$, as well as topological properties of the class $\tilde{A}(D)$ endowed with its natural metric topology. More generally, we examine analogous questions replacing $\mathbb{C} \cup \{\infty\}$ by an arbitrary metrizable compactification of \mathbb{C} and replacing the closed unit disc \overline{D} by other compact sets (Mergelyan's theorem). The set of universal Taylor series in the sense of Luh and Chui and Parnes contained in $\tilde{A}(D)$ is G_{δ} and dense in $\tilde{A}(D)$. Are there any such universal series in $\tilde{A}(D) \setminus A(D)$, where A(D)denotes the classical disc algebra?

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