

CONFÉRENCE « ESPACES DE HILBERT DE FONCTIONS ANALYTIQUES »  
8–12 DÉCEMBRE 2008

CONFERENCE ON HILBERT SPACES OF ANALYTIC FUNCTIONS  
DECEMBER 8–12, 2008

## Approximation of $\zeta(s)$ and $\zeta'(s)$ by the Riemann zeta-function

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With Clouâtre, we have shown that any holomorphic function can be approximated by translates of Taylor polynomials of the Riemann zeta-function. On the other hand, with Zeron, we have shown that the Riemann zeta-function can be approximated by functions for which the analogue of the Riemann hypothesis fails. Recently, with Xarles, we have shown that it can also be approximated by functions for which the analogue of the Riemann hypothesis holds.